



Module 5



Basics of energy conversation cycles



Heat Engines and Efficiencies



- The objective is to build devices which receive heat and produce work (like an aircraft engine or a car engine) or receive work and produce heat (like an air conditioner) in a sustained manner.
- All operations need to be cyclic. The cycle comprises of a set of processes during which one of the properties is kept constant (V, p, T etc.)



Heat Engines (contd...)

- A minimum of 3 such processes are required to construct a cycle.
- All processes need not have work interactions (eg: isochoric)
- All processes need not involve heat interactions either (eg: adiabatic process).



Heat Engines (Contd...)



- A cycle will consist of processes: involving some positive work interactions and some negative.
- If sum of +ve interactions is $>$ -ve interactions the cycle will produce work
- If it is the other way, it will need work to operate.
- On the same lines some processes may have +ve and some -ve heat interactions.



Heat Engines (Contd...)

- Commonsense tells us that to return to the same point after going round we need at one path of opposite direction.
- I law does not forbid all heat interactions being +ve nor all work interactions being -ve.
- But, we know that you can't construct a cycle with all +ve or
- All -ve Q's nor with all +ve or all -ve W's
- Any cycle you can construct will have some processes with
- Q +ve some with -ve.



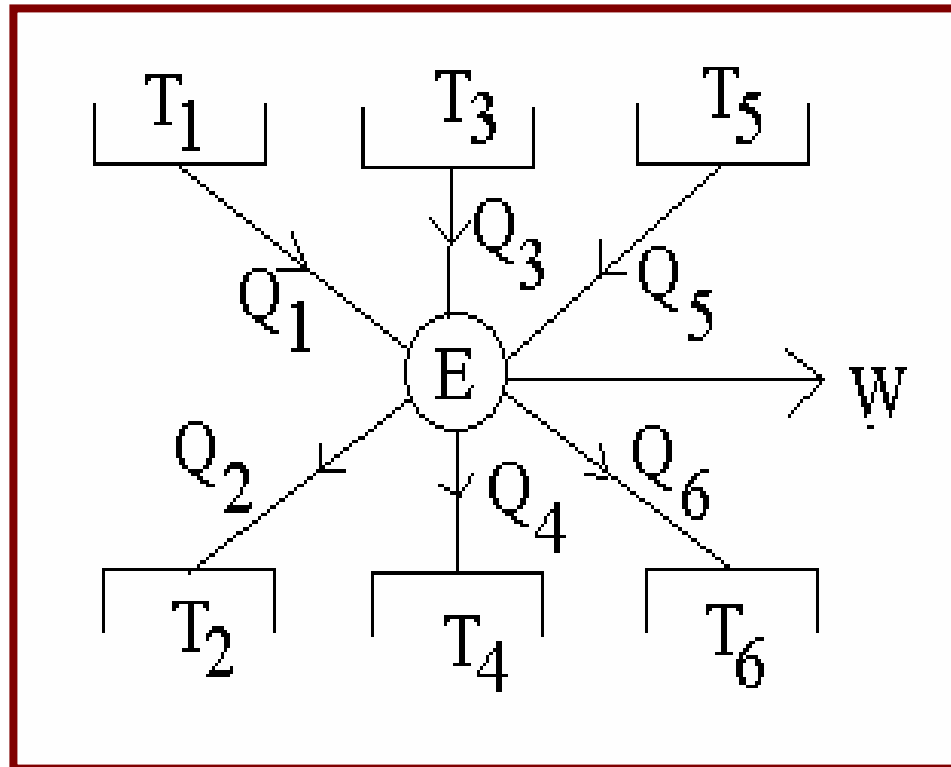
Heat Engines (Contd...)



- Let $Q_1, Q_3, Q_5 \dots$ be +ve heat interactions (Heat supplied)
- $Q_2, Q_4, Q_6 \dots$ be -ve heat interactions (heat rejected)
- From the first law we have
- $Q_1 + Q_3 + Q_5 \dots - Q_2 - Q_4 - Q_6 \dots = \text{Net work delivered } (W_{\text{net}})$
- $\Sigma Q_{+ve} - \Sigma Q_{-ve} = W_{\text{net}}$
- The efficiency of the cycle is defined as $\eta = W_{\text{net}} / \Sigma Q_{+ve}$
- Philosophy → What we have achieved ÷ what we have spent to achieve it



Heat Engines (Contd...)





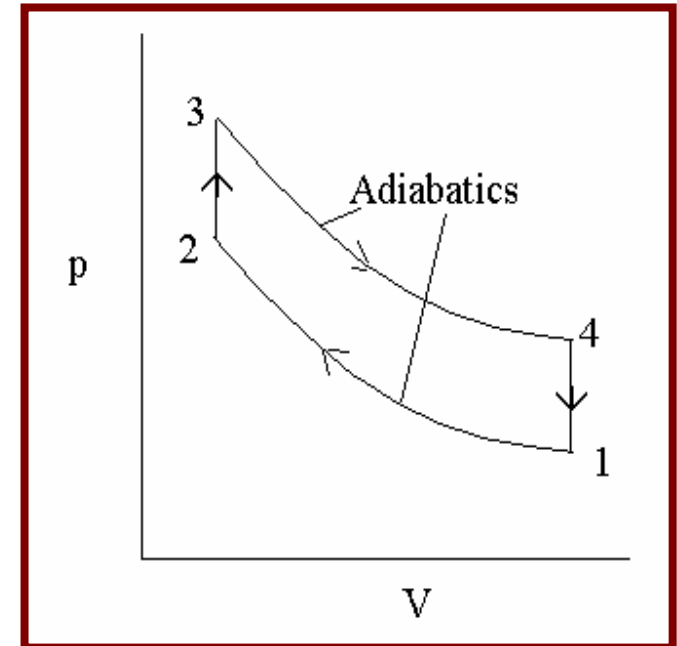
Otto Cycle



Consider the **OTTO Cycle** (on which your car engine works)

It consists of two isochores and two adiabatics

- There is no heat interaction during 1-2 and 3-4
- Heat is added during constant volume heating (2-3) $Q_{2-3} = c_v (T_3 - T_2)$
- Heat is rejected during constant volume cooling (4-1) $Q_{4-1} = c_v (T_1 - T_4)$
Which will be negative because $T_4 > T_1$





Otto Cycle (Contd...)



- Work done = $c_v (T_3 - T_2) + c_v (T_1 - T_4)$
- The efficiency = $\frac{[c_v(T_3 - T_2) + c_v(T_1 - T_4)]}{[c_v(T_3 - T_2)]}$
 $= \frac{[(T_3 - T_2) + (T_1 - T_4)]}{[(T_3 - T_2)]}$
 $= 1 - \frac{(T_4 - T_1)}{(T_3 - T_2)}$



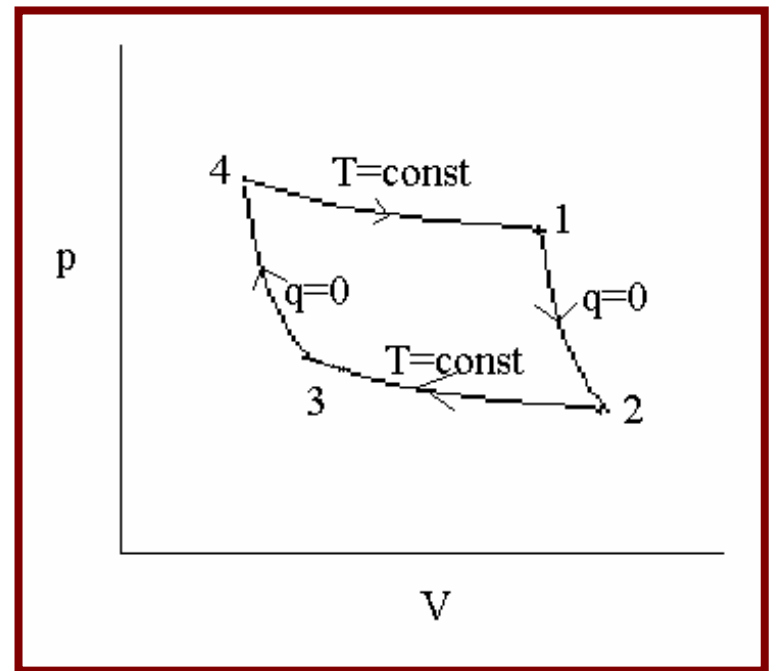
Carnot Cycle



Consider a **Carnot cycle** - against which all other cycles are compared

It consists of two isotherms and two adiabatics

- Process 4-1 is heat addition because $v_4 < v_1$
- Process 2-3 is heat rejection because $v_3 < v_2$





Carnot Cycle (contd..)



<u>Process</u>	<u>Work</u>	<u>Heat</u>
1-2	$(p_1v_1 - p_2v_2)/(g-1)$	0
2-3	$p_2v_2 \ln (v_3/v_2)$	$p_2v_2 \ln (v_3/v_2)$
3-4	$(p_3v_3 - p_4v_4)/(g-1)$	0
4-1	$p_4v_4 \ln (v_1/v_4)$	$p_4v_4 \ln (v_1/v_4)$
Sum	$(p_1v_1 - p_2v_2 + p_3v_3 - p_4v_4)/(g-1)$	
	$+ RT_2 \ln (v_3/v_2)$	$RT_2 \ln (v_3/v_2)$
	$+ RT_1 \ln (v_1/v_4)$	$+ RT_1 \ln (v_1/v_4)$

But, $p_1v_1 = p_4v_4$ and $p_2v_2 = p_3v_3$

Therefore the first term will be 0

!!We reconfirm that I law works!!



Carnot Cycle (contd..)



We will show that $(v_2/v_3) = (v_1/v_4)$

1 and 2 lie on an adiabetic

so do 3 and 4

$$p_1 v_1^{\gamma} = p_2 v_2^{\gamma}$$

$$p_4 v_4^{\gamma} = p_3 v_3^{\gamma}$$

Divide one by the other
 $/p_3 v_3^{\gamma}$ (A)

$$(p_1 v_1^{\gamma} / p_4 v_4^{\gamma}) = (p_2 v_2^{\gamma} / p_3 v_3^{\gamma})$$

$$(p_1/p_4) (v_1^{\gamma} / v_4^{\gamma}) = (p_2/p_3) (v_2^{\gamma} / v_3^{\gamma})$$

But $(p_1/p_4) = (v_4/v_1)$ because 1 and 4 are on the same isotherm

Similarly $(p_2/p_3) = (v_3/v_2)$ because 2 and 3 are on the same isotherm



Carnot Cycle (contd..)



Therefore A becomes

$$(v_1 / v_4)^{\gamma-1} = (v_2/v_3)^{\gamma-1}$$

which means

$$(v_2/v_3) = (v_1/v_4)$$

Work done in Carnot cycle = $RT_1 \ln (v_1/v_4) + RT_2 \ln (v_3/v_2)$

$$= RT_1 \ln (v_1/v_4) - RT_2 \ln (v_2/v_3)$$

$$= R \ln (v_1/v_4) (T_1 - T_2)$$

Heat supplied = $R \ln (v_1/v_4) T_1$

The efficiency = $(T_1 - T_2)/T_1$

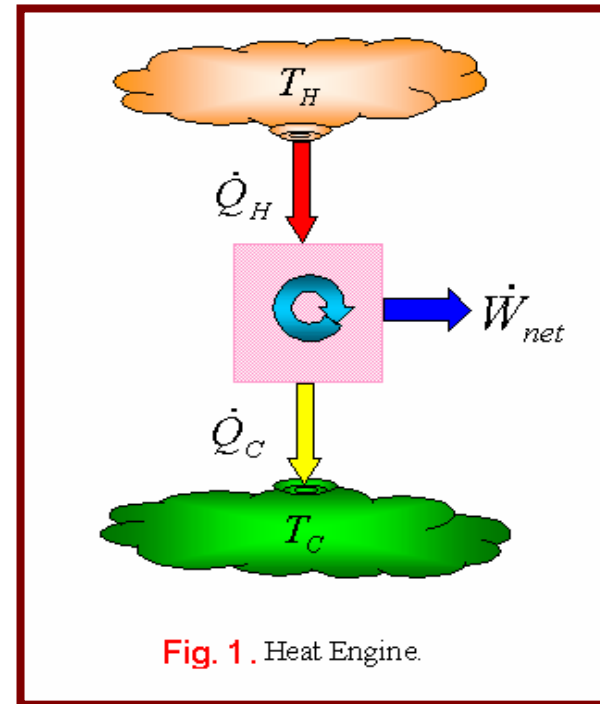
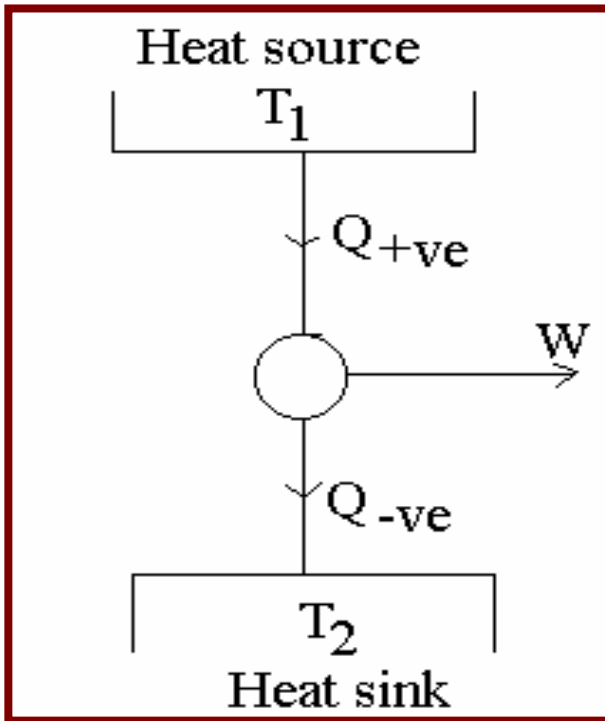
In all the cycles it also follows that Work done = Heat supplied - heat rejected



Carnot Cycle (contd..)

Carnot engine has one $Q +ve$ process and one $Q -ve$ process. This engine has a single heat source at T_1 and a single sink at T_2 .

If $Q +ve > Q -ve$; W will be $+ve$ It is a heat engine





Carnot Cycle (contd..)



It will turn out that Carnot efficiency of $(T_1 - T_2)/T_1$ is the best we can get for any cycle operating between two fixed temperatures.



Carnot Cycle (contd..)



$Q_{+ve} < Q_{-ve}$ W will be -ve It is not a heat engine

Efficiency is defined only for a work producing heat engine
not a work consuming cycle

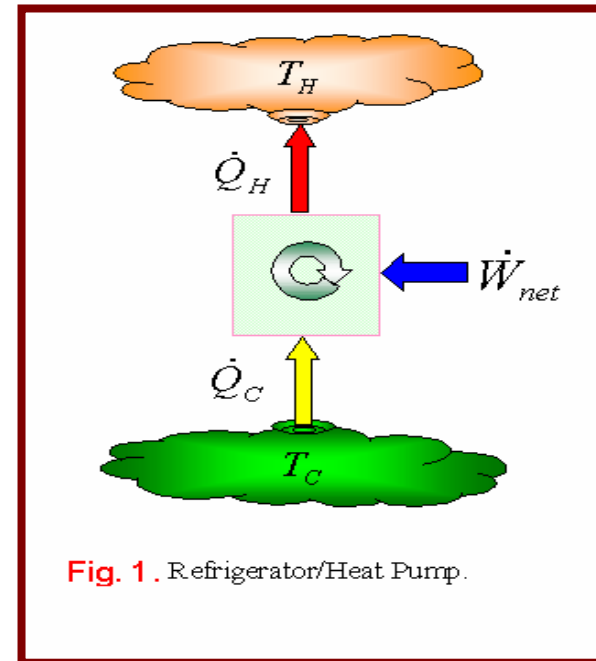
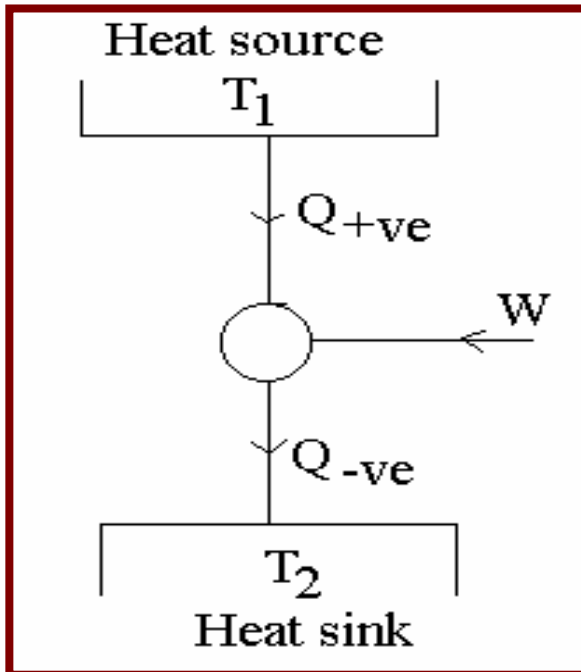


Fig. 1. Refrigerator/Heat Pump.



Carnot Cycle (contd..)



Note: We can't draw such a diagram for an Otto cycle because there is no single temperature at which heat interactions occur